L-Band SiGe HBT Active Differential Equalizers with Variable, Positive or Negative Gain Slopes Using Dual-Resonant RLC Circuits

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Abstract

L-band SiGe HBT active differential equalizers with variable, positive or negative gain slopes have been designed and fabricated for frequency and temperature compensation of microwave and optical systems. The active equalizer employs dual-resonant RLC circuits in the series feedback path of the differential amplifier for positive gain slopes or in the load for negative gain slopes. The implemented active equalizers have achieved positive gain slopes of +54 to +87 dB/GHz across 0.2 to 0.6 GHz as well as negative gain slopes of -50 to -100 dB/GHz over 0.6 to 1.2 GHz. The active differential equalizers presented in this paper have an outstanding feature of providing variable, positive or negative gain slopes, which can be easily adjusted to meet with various stringent requirements for frequency and temperature compensation in microwave and optical systems.

1. Introduction

First of all, this paper is an extension of the work originally presented in the 46th European Microwave Conference, 2016 [1]. The research and development of active equalizers have started at the beginning of 1970s as active RC filters with IC operational amplifiers in the audio band because of having many advantages over passive equalizers in terms of inductor-less, cheaper, smaller, easily manufactured and tuned circuits [2]. Since then, various types of active, adjustable amplitude and delay equalizers have been developed, including classical Bode variable equalizers, transfer-function types and switched-capacitor equalizers [3, 4, 5]. With the tremendous growth in semiconductor NMOS, CMOS devices, the R&D activities of active equalizers have moved toward wideband, high speed data transmission systems, a variety of analog adaptive equalizer architectures have been developed to eliminate signal distortions [6, 7, 8, 9]. Meanwhile, wideband microwave and optical receivers have been long tackled with the insertion loss seriously large. To address this problem, many authors have presented various types of the active equalizer with variable, positive or negative gain slopes. The advanced feature is that active devices are used as an amplifier in place of the conventional switching or variable-capacitance device to achieve high gain. Moreover, to achieve higher frequency operation as well as miniaturized size, LC-resonators in place of the traditional RC filters are employed in the series feedback path or load circuit of the differential amplifier for positive or negative gain slopes. The active differential equalizers are as follows: Capacitance-selectable bridged-T attenuators were incorporated into the series feedback path to achieve variable positive gain slope, which can be digitally controlled [14]. Series LC resonators were employed in the base or collector bias circuits to realize variable, positive or negative gain slopes [15]. Single-band series or parallel LC resonators were used in the feedback path of the differential amplifier for the same purposes [16]. These active equalizers, however, can vary gain slopes but the frequency positions were fixed. To overcome this problem, a novel active differential equalizer having variable inclination and position of the positive or negative gain slopes have been presented in [1]. It employs dual-resonant RLC circuits in the feedback path of the differential amplifier for positive gain slopes or in the load for negative gain.
slopes. To extend the work, the theory and design for the active differential equalizer using the dual-resonant RLC circuits are described in more detail. Then the circuit design, simulation and performance are newly added for the case that dual capacitors (actually two varactor diodes) consisting of the dual-resonant RLC circuit are independently varied. These active differential equalizers are relatively narrowband as well as provide abrupt gain slopes but can be easily extended to wideband design with the proper choice of circuit parameters.

2. Active Differential Equalizer Using Dual-Resonant RLC Circuits

Two types of the active differential equalizers with variable inclination and position of the positive or negative gain slopes are graphically shown in Figure 1. $f_{BP}$ and $f_{BN}$ are peak frequencies. $f_{BP}$ and $f_{BN}$ are bandstop frequencies. The conventional active equalizers [14, 15, 16] can vary either a peak or bandstop frequency. Thus only gain slope can be varied. On the other hand, the novel active equalizers can vary both peak and bandstop frequencies. Thus both the inclination and position of gain slopes can be varied.

![Figure 1](image1)

Figure 1 Two types of the active differential equalizers with variable inclination and position of the positive or negative gain slopes

![Figure 2](image2)

Figure 2 Schematic diagram of the differential amplifier and dual-resonant RLC circuit

Schematic diagrams of the differential amplifier and dual-resonant RLC circuit are shown in Figure 2. The dual-resonant circuit consists of series LC ($L_2$, $C_2$) and parallel LC ($L_1$, $C_1$) circuits combined with a resistor ($R_S$ or $R_L$). The dual-resonant RLC circuit becomes purely resistive at the frequency $f_1$ and $f_2$, which are given as follows:

$$f_1 = \frac{1}{2\pi} \sqrt{\frac{b + \sqrt{b^2 - 4a}}{2a}}$$  \quad (1)

$$a = L_1 L_2 C_1 C_2$$  \quad (3)

$$b = L_1 C_1 + L_2 C_2 + L_2 C_2$$  \quad (4)

The circuit also becomes short-circuited at the frequency $f_3$.

$$f_3 = \frac{1}{2\pi \sqrt{L_2 C_2}}$$  \quad (5)

The voltage gain of the differential amplifier ($G_V$) in Figure 2(a) can be approximated as the following equation, where $Z_L$ and $Z_S$ are an impedance of the load and feedback circuits.

$$G_V = \frac{Z_L}{Z_S}$$  \quad (6)

When the dual-resonant RLC circuit is applied to $Z_S$, $G_V$ becomes minimum at $f_1$ and $f_2$ as well as maximum at $f_3$, which is graphically shown in Figure 3(a). Whereas, when the dual-resonant RLC circuit is applied to $Z_L$, $G_V$ becomes maximum at $f_1$ and $f_2$ as well as minimum at $f_3$, which is graphically shown in Figure 3(b). The differential amplifier provides variable, positive gain slopes ($G_P$) between $f_1$ and $f_3$ by adjusting $f_1$ or $f_3$. Actually, $f_1$ or $f_3$ can be varied with $C_1$ or $C_2$. It must be noted here that both $f_1$ and $f_3$ can be varied with $C_1$. Meanwhile, the differential amplifier produces variable, negative gain slopes ($G_N$) between $f_1$ and $f_3$ by adjusting $f_1$ or $f_3$. In the similar way, $f_1$ or $f_3$ can be varied with $C_1$ or $C_2$. However, it must be also noted that both $f_1$ and $f_3$ can be varied with $C_1$.

![Figure 3](image3)

Figure 3 Voltage gains of the differential amplifier when the dual-resonant RLC circuit is applied to $Z_S$ or $Z_L$. 

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The resonant frequencies $f_1$, $f_2$ and $f_3$ are calculated by using (1) to (5) and are shown in Figure 4. The circuit element values are listed in Table 1. It is clearly shown that the inclination and position of positive or negative gain slopes can be tuned by varying $C_1$, $C_2$ or both. As described above, $f_1$ and $f_3$ cannot be varied independently with $C_2$ changes in Figure 4(b).

### 3. Circuit Design

Schematic diagrams of the active differential equalizer with variable, positive or negative gain slopes are displayed in Figures 5 and 6, respectively. Dual-resonant RLC circuits are employed in the feedback path of the differential amplifier for positive gain slopes or in the load for negative gain slopes.

![Schematic diagram of the active differential equalizer with variable, positive gain slopes](image)

**Figure 5** Schematic diagram of the active differential equalizer with variable, positive gain slopes

![Schematic diagram of the active differential equalizer with variable, negative gain slopes](image)

**Figure 6** Schematic diagram of the active differential equalizer with variable, negative gain slopes

As shown in Figure 2(b), the dual-resonant RLC circuit consists of a series LC circuit ($L_2$, $C_2$), a parallel LC circuit ($L_1$, $C_1$) and a resistor ($R_5$ or $R_6$). $R_5$ or $R_6$ plays an important role of circuit stability and impedance matching. $R_L$ is basically chosen as 50 ohms for impedance matching. But $R_5$ has to be carefully determined to achieve both high stability and high gain. When the dual-resonant RLC circuit is employed in $Z_S$, $R_L$ is used in $Z_L$. Meanwhile, the dual-resonant RLC circuit is employed in $Z_L$, $R_S$ is utilized in $Z_S$.

Now the voltage gain with positive gain slopes ($G_p$) and that with negative gain slopes ($G_n$) can be given from (6) as follows:

$$G_p = R_L \sqrt{\text{Re}[Y_s]^2 + \text{Im}[Y_s]^2}$$

(7)

$$\text{Re}[Y_s] = \frac{1}{R_S}$$

(8)

---

Table 1 Circuit element values

<table>
<thead>
<tr>
<th>Element</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$R_L$ [Ω]</td>
<td>56</td>
</tr>
<tr>
<td>$R_S$ [Ω]</td>
<td>10</td>
</tr>
<tr>
<td>$L_1$ [nH]</td>
<td>100</td>
</tr>
<tr>
<td>$C_1$ [pF]</td>
<td>6 to 15</td>
</tr>
<tr>
<td>$L_2$ [nH]</td>
<td>1</td>
</tr>
<tr>
<td>$C_2$ [pF]</td>
<td>6 to 15</td>
</tr>
</tbody>
</table>
G_\text{P} \text{ and } G_\text{N} \text{ are calculated by using (7) to (12) and the circuit element values in Tables 1. The calculation was done for variable } C_1 \text{ and fixed } C_2 \text{ or variable } C_2 \text{ and fixed } C_1. \text{ The calculated } G_\text{P} \text{ and } G_\text{N} \text{ are plotted in Figures 7 and 8, respectively. It is clearly demonstrated that variable, positive or negative gain slopes can be obtained. Due to a large value of } L_1, \text{ a variation of the bandstop frequency } f_1 \text{ is small in Figure 7. Thus the positive gain slopes greatly change with } f_2 (C_2) \text{ in Figure 7(b). In the similar way, due to a large value of } L_1, \text{ a variation of the bandstop frequency } f_1 \text{ is also small in Figure 8. The negative gain slopes largely vary with } f_2 (C_2) \text{ in Figure 8(b).}

\begin{align*}
\text{Im}[Y_L] &= \text{Im}[Y_L] \\
G_N &= \frac{1}{R_S \sqrt{\text{Re}[Y_L]^2 + \text{Im}[Y_L]^2}} \\
\text{Re}[Y_L] &= \frac{1}{R_L} \\
\text{Im}[Y_L] &= \frac{\omega^4 L_2 L_2 C_1 C_2 - \omega^4 (L_2 C_1 + L_2 C_2 + L_2 C_2) + 1}{\omega L_2 (1 - \omega^2 L_2 C_2)}
\end{align*}

Figure 7 Calculated G_\text{P} \text{ for variable } C_1 \text{ and fixed } C_2 \text{ or variable } C_2 \text{ and fixed } C_1

Figure 8 Calculated G_\text{N} \text{ for variable } C_1 \text{ and fixed } C_2 \text{ or variable } C_2 \text{ and fixed } C_1

Figure 9 Simulated gains of the active differential equalizer with variable, positive gain slopes
mount type of the varactor diode with a capacitance ratio of 2.5 (Toshiba 1SV279) was used. The circuit size is 14 x 16 x 1.2 mm³.

Figure 11 Photographs of the active differential equalizer with variable, positive or negative gain slopes

6. Circuit Performance

The measured gains of the active differential equalizers are plotted in Figure 12 for the positive gain slopes and in Figure 13 for the negative gain slopes. The measurement was done for variable C₁ and fixed C₂ or variable C₂ and fixed C₁. Actually C₁ or C₂ was varied with a control voltage V_{C1} or V_{C2} of the varactor diode. The measurement conditions are shown in Figures 12 and 13, respectively.

Figure 12 Measured gains of the active differential equalizer with variable, positive gain slopes

5. Circuit Fabrication

Photographs of the active differential equalizer with variable, positive or negative gain slopes are shown in Figure 11. The active differential equalizers were fabricated on the FR-4 substrate with a dielectric constant of 4.5. 0.35µm SiGe HBTs with an fᵢ of 25GHz (Toshiba MT4S102T), 1005-type resistors, inductors and capacitors are mounted on the substrate by soldering. A surface
1.6
unknown
plusmin 30dB/GHz
Amplifier
Equalizer Type
0.4
1.0
Active Device
0.8
1.4
method for Receiver Active
Positive, Negative
Gain Slope
plusmin 16dB/GHz
1.6
Bridged-T
qualizers”, IEEE Trans.
GaAs
Role
Variable R
-thod for Receiver Active
Positive, Negative
Swiching
Positive, Negative
PIN Diode
<-2dB
0.8
, which can be easily
-
0.67dB/GHz
Filter


Table 2: Summary of performances of active equalizers

<table>
<thead>
<tr>
<th>Ref</th>
<th>Active Device</th>
<th>Role</th>
<th>Equalizer Type</th>
<th>Circuit Topology</th>
<th>Frequency Band</th>
<th>Gain Slope</th>
<th>Gain</th>
</tr>
</thead>
<tbody>
<tr>
<td>[10]</td>
<td>GaAs MESFET</td>
<td>Switching</td>
<td>Negative Slope</td>
<td>Bridge-T</td>
<td>DC - 18GHz</td>
<td>-0.67dB/GHz</td>
<td>&lt;2.7dB</td>
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</table>

The work 0.35 micron SiGe HBT Amplifier Positive, Negative Amplifier Positive, Negative Slope Differential Active Equalizer

Conclusions

Two types of the active differential equalizers with variable, positive or negative gain slopes have been presented. With the use of the dual-resonant RLC circuit in the feedback or load circuit, the active differential equalizers have achieved positive gain slopes of +54 to +87dB/GHz across 0.2 to 0.6GHz as well as negative gain slopes of -50 to -100dB/GHz over 0.6 to 1.2GHz. The active differential equalizers presented in this paper show narrow bandwidth but abrupt gain slopes, which can be easily extended to wide bandwidth and moderate gain slopes with the proper choice of the circuit parameters. Moreover, the input and output matches can be improved with the use of a lossy match structure. It can be concluded from these results that the active differential equalizers would be one candidate for frequency and temperature compensations in microwave and optical systems.

References


7. Conclusions

The active differential equalizer with variable, positive gain slopes has achieved a gain slope of +50 to +70dB/GHz over 0.2 to 0.6GHz in Figure 12(a) as well as +54 to +87dB/GHz across 0.2 to 0.6GHz in Figure 12(b). The input and output return losses were better than 2dB and 15dB, respectively, which can be easily improved by employing a lossy match circuit in the input matching circuit.

The active differential equalizer with variable, negative gain slopes has achieved a gain slope of -55 to -95dB/GHz over 1.1 to 1.5GHz in Figure 13(a) as well as -50 to -100dB/GHz across 0.6 to 1.2GHz in Figure 13(b). The input and output return losses were better than 2dB. In a similar way as the positive gain slope, the input and output matches can be further improved with the use of a lossy match configuration.

These performances were compared with the conventional active equalizers and summarized in Table 2. It is clearly shown that the active differential equalizers presented in this paper can provide narrow-band but abrupt gain slopes as well as higher gain. With the proper choice of the circuit parameters, it is very easy to meet with the moderate gain slopes over a wide bandwidth.


